## Selected Symbols for Basic Mathematical/Statistical Modeling

These are the key mathematical symbols (other than $+,-, \cdot, /,=$, etc.) used in "Mathematical Models \& Linear Statistical Models: Basic Concepts \& Computations".

| Concept | Symbol | Definition | Examples |
| :---: | :---: | :---: | :---: |
| Floor | \...」 | Rounding down (towards $-\infty$ ) of a non-integral real number, to the next integer value. | $\begin{aligned} \lfloor 1.75\rfloor & =1 \\ \lfloor-1.75\rfloor & =-2 \\ \lfloor 1\rfloor & =1 \end{aligned}$ |
| Ceiling | †...] | Rounding up (towards $\infty$ ) of a non-integral real number, to the next integer value. | $\begin{aligned} \lceil 1.75\rceil & =2 \\ \lceil-1.75\rceil & =-1 \\ \lceil 1\rceil & =1 \end{aligned}$ |
| Exponent | $b^{n}$ (superscript) | Number of times (not necessary integral) a base $b$ is multiplied by itself in a product. | $\begin{aligned} x^{2} & =x \cdot x \\ 3^{4} & =3 \cdot 3 \cdot 3 \cdot 3=81 \end{aligned}$ |
| Enumeration | $\begin{gathered} S_{i} \\ \text { (subscript) } \end{gathered}$ | Numbered terms of an ordered sequence. | $\begin{aligned} \boldsymbol{S} & =\left\{s_{1}, s_{2}, s_{3}, \ldots\right\} \\ \boldsymbol{F} & =\{1,1,2,3,5, \ldots\} \end{aligned}$ <br> ( $\boldsymbol{F}$ is Fibonacci sequence.) |
| Sum | $\sum$ | Sum of terms in a sequence. $\sum_{i=m}^{n} s_{i}=s_{m}+s_{m+1}+\ldots+s_{n}$ <br> (If the bounds $m$ and $n$ are well understood, they are often omitted from the $\sum$ operator notation.) | $\begin{aligned} \sum_{i=1}^{4} f_{i} & =f_{1}+f_{2}+f_{3}+f_{4} \\ & =1+1+2+3 \end{aligned}$ <br> (Sum of $1^{\text {st }} 4$ terms of Fibonacci sequence.) |
| Product | $\prod$ | Product of terms in a sequence. $\prod_{i=m}^{n} s_{i}=s_{m} \cdot s_{m+1} \cdot \ldots \cdot s_{n}$ | $\begin{aligned} \prod_{i=3}^{5} \frac{i}{i+1} & =\frac{3}{4} \cdot \frac{4}{5} \cdot \frac{5}{6} \\ & =\frac{1}{2} \end{aligned}$ |
| Factorial | $n$ ! | $\begin{aligned} n! & =\prod_{i=1}^{n} i \\ & =1 \cdot 2 \cdot \ldots \cdot n \\ 0! & =1 \end{aligned}$ | $\begin{aligned} 5! & =1 \cdot 2 \cdot 3 \cdot 4 \cdot 5 \\ & =120 \end{aligned}$ |
| Euler's number | $e$ | Base of natural logarithms. $\begin{aligned} e & =\sum_{i=0}^{\infty} \frac{1}{n!} \\ & =\frac{1}{0!}+\frac{1}{1!}+\frac{1}{2!}+\frac{1}{3!}+\ldots \\ & \approx 2.71828 \ldots \end{aligned}$ |  |

